

xpts =

-3.0000

0

0.3333

1.0000

4.0000

The derivative $u'(2)$ of u at $x_b = 0.5$ is approximated by

$$\begin{aligned} & -5.952380952380953e-03 * u(x(1)) + \\ & 6.166666666666667e+00 * u(x(2)) + \\ & -9.204545454545451e+00 * u(x(3)) + \\ & 3.041666666666666e+00 * u(x(4)) + \\ & 2.164502164502167e-03 * u(x(5)) + \end{aligned}$$

Actual Error = 0.000158771

For smooth u ,

$$\text{Estimated Error} = -0.0347222 * u^{(5)}(0.5) + (-0.00947145) * u^{(6)}(0.5) + \dots$$