

Math 495R Homework 23

- (1) Project Euler, problem 10
- (2) Project Euler, problem 25
- (3) A) For each number  $n$  from 3 to 100, compute the value of  $2^{n-1} \pmod{n}$ . When is this congruent to 1  $\pmod{n}$ ?  
B) Now choose a prime number  $p$  between 20 and 100. For each number  $n$  between 1 and  $p-1$ , determine the smallest positive power  $k$  such that  $n^k \equiv 1 \pmod{p}$ , if there is one. What do you notice about these powers? Repeat this for two other primes.