Homework 10, due September 25

(1) (Page 147, Problem 6) Suppose Triple DES is performed by choosing two keys $K_1, K_2$ and computing $E_{K_1}(E_{K_2}(E_{K_2}(m)))$. Note that the order of the keys has been changed from the usual two-key Triple DES. Show how to attack this modified version with a meet-in-the-middle attack.

(2) New codebook: ROT3. Let us invent our own codebook, called ROT3. The key $k$ and input $x$ are both 3-bit binary numbers. Define the output to be $ROT3(k, x) = k \oplus \text{RotateLeft}(x)$, where RotateLeft($x$) cyclically rotates by 1 bit to the left. Note: the plaintext gets rotated, not the key. For example, $ROT3(011, 100) = 011 \oplus \text{RotateLeft}(100) = 011 \oplus 001 = 010$. You find the inverse codebook to ROT3 yourself.

Let’s use the ROT3 codebook above. Suppose we use the key 101 and plaintext 000111101. What is the ciphertext in each of the following modes?

(a) Electronic Codebook mode (ECB).
(b) Cipher Block Chaining mode (CBC) using an Initial Value of 110.
(c) Cipher Feedback mode using Initial Value 110. ($O_j$ and $X_j$ should be 3 bits long.)
(d) Output Feedback mode using Initial Value 110. ($O_j$ and $X_j$ should be 3 bits long.)
(e) Counter Mode (CTR) using Initial Value 110. (Note that 111 + 1 = 000, as we are working with 3-bit binary numbers.)

(3) As in the previous problem, let us use the ROT3 codebook. Suppose we use the key 101 and ciphertext 101111000. Decrypt to get the plaintext if the message was sent in the following mode. Draw diagrams to show your work.

(a) Electronic Codebook mode (ECB).
(b) Cipher Block Chaining mode (CBC) using an Initial Value of 110.
(c) Cipher Feedback mode using Initial Value 110.
(d) Output Feedback mode using Initial Value 110.
(e) Counter Mode (CTR) using Initial Value 110.